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Contribution of the finite volume point dilution method for measurement of groundwater fluxes in a fractured aquifer



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ABSTRACT

Measurement of groundwater fluxes is the basis of all hydrogeological study, from hydraulic characterization to the most advanced reactive transport modeling. Usual groundwater flux estimation with Darcy's law may lead to cumulated errors on spatial variability, especially in fractured aquifers where local direct measurement of groundwater fluxes becomes necessary. In the present study, both classical point dilution method (PDM) and finite volume point dilution method (FVPDM) are compared on the fractured crystalline aquifer of Ploemeur, France. The manipulation includes the first use of the FVPDM in a fractured aquifer using a double packer. This configuration limits the vertical extent of the tested zone to target a precise fracture zone of the aquifer. The result of this experiment is a continuous monitoring of groundwater fluxes that lasted for more than 4 days.

Measurements of groundwater flow rate in the fracture (Q_t) by PDM provide good estimates only if the mixing volume (V_w) (volume of water in which the tracer is mixed) is precisely known. Conversely, the FVPDM allows for an independent estimation of V_w and Q_t , leading to better precision in case of complex experimental setup such as the one used. The precision of a PDM does not rely on the duration of the experiment while a FVPDM may require long experimental duration to guarantees a good precision.

Classical PDM should then be used for rapid estimation of groundwater flux using simple experimental setup. On the other hand, the FVPDM is a more precise method that has a great potential for development but may require longer duration experiment to achieve a good precision if the groundwater fluxes investigated are low and/or the mixing volume is large.

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1. Introduction

Estimation of groundwater fluxes remains the basis of all hydrogeological study, from hydraulic characterization to the most advanced reactive transport modeling. Investigations on contaminant behavior, design of remediation systems, groundwater–surface water interactions or geothermal applications, all would benefit from a precise quantification of

* Corresponding author. E-mail address: Serge.Brouyere@ulg.ac.be (S. Brouyère). groundwater fluxes and their temporal and spatial variability. Groundwater fluxes are usually indirectly calculated with Darcy's law from piezometric gradient measurements and the estimation of hydraulic conductivity with pumping/slug tests. This simple method may be adequate for the estimation of general groundwater fluxes in homogeneous media but the resolution is generally low, leading to cumulated errors on spatial variability in heterogeneous context (Bright et al., 2002; Devlin and McElwee, 2007).

Estimation of groundwater fluxes in fractured aquifer is a challenge given the heterogeneity that is induced by discrete fractures (Novakowski, 2006). The characterization of fracture flow based on hydraulic pressure measurements can actually lead to misinterpretation about the role of the fracture in terms of flow path and solute transport. For example, a dead-end fracture subjected to pumping will respond in terms of hydraulic pressure variations even if no groundwater flow is occurring. Zha et al. (2014) recently emphasized that flux data used in hydraulic characterization of fractured media improve estimation of fracture patterns and hydraulic conductivity fields.

Therefore, tracer tests become essential tools because they allow studying the actual displacement of water. Classical tracer tests provide averaged information between two injection and recovery points. Alternative methods, such as point dilution tracer tests are promising to obtain a direct measurement of local groundwater fluxes or Darcy fluxes (q_D) (Halevy et al., 1967; Klotz et al., 1979; Zlotnik and Zurbuchen, 2003; Brainerd and Robbins, 2004; Hatfield et al., 2004; Huang and Goltz, 2005; Pitrak et al., 2007; West and Odling, 2007; Sale et al., 2007). Novakowski et al. (1995 and 2006) performed classical dilution tests between packers and pointed out two major issues. The first issue is related to the estimation of the actual mixing volume (V_w) , which has to be accurately known to interpret the dilution test. This mixing volume is difficult to calculate in the case of dilution test performed between the packers because the test space is full of equipment (hoses, probes, mixing propellers ...) and may include zone of immobile water. Furthermore, the geometry of the borehole in front of the tested zone may not be perfectly cylindrical and part of the adjacent fractured medium may also be involved in the mixing processes. The second issue is that groundwater velocity changed during their experiments and disturbed the recording. The point dilution method (PDM) is actually a short time experiment that is constrained by both the maximum concentration that can be injected and the minimum concentration that can be measured in the well. The experiment stops when the entire amount of tracer has been eluted from the well, precluding continuous monitoring of groundwater fluxes.

The finite volume point dilution method (FVPDM) (Brouyère, 2003; Brouyère et al., 2005; Brouyère et al., 2008) allows overcoming those two issues and provides a quantification by a simultaneous and independent estimation of the mixing volume (V_w) and Darcy's flux (q_D) on experimental data. The duration of the test is not limited and can last as long as the experiment is maintained active by injecting tracer and monitoring its concentrations in the mixed water volume. Measurements of groundwater flux at a local scale, as achieved with this method, are complementary with more regional and indirect estimations from Darcy's law. The method was tested successfully in porous media (Brouyère et al., 2008; Goderniaux et al., 2010), but has never been experienced in fractured aquifers.

In this context, the objectives of this paper are twofold: (1) test the method in a fractured geological context; and (2) compare the FVPDM with classical PDM on the same experimental site, hydraulic conditions, and experimental setup. The comparison investigates the relative precision of the two techniques on the measurement of groundwater fluxes and it provides guidelines for dilution experiments in fractured media. The contribution of the FVPDM for groundwater flux measurement in fractured aquifer is also discussed in terms of experimental setup.

A series of tracer dilution experiments were performed in the Ploemeur test site (Britany, France) on several fractured zones of an open well. For the first time, the FVPDM was used between a double-packer system to investigate localized groundwater flows in discrete fractures. Successive experiments were carried out with different pumping rates applied at a nearby well, to investigate the largest range of possible groundwater flux measurements, and to study the consistency of results over this range. Classical PDM was also performed following each FVPDM experiment to compare the sensitivity and uncertainties of both methods. After a description of the methodology and the experimental setup, the results of the groundwater flux measurements are discussed along with uncertainties on the interpretation of the FVPDM and PDM.

2. Methodology

2.1. Point dilution techniques

The aim of a single borehole dilution test is to perform a direct measurement of groundwater fluxes. Point dilution methods relate the concentration evolution of a tracer previously injected in a borehole as a function of the intensity of groundwater flow through the screen of the borehole. The result of such test is a groundwater flux, which depends on the hydraulic conditions within the geological formation and in the vicinity of the tested borehole (Drost et al., 1968; Hall, 1996). Since the first use of PDM in 1916 reported by Halevy et al. (1967), many PDM configurations have been tested, including the experiments by Kaufmann and Todd (1962) and Novakowski et al. (1998, 2006), using inflatable packers to limit the vertical extension of the investigated zone. The tracer can be salt species, fluorescent dyes or radio isotopes (Klotz et al., 1979).

The finite volume point dilution method (FVPDM) generalizes the PDM to more advanced tracer injection scenarios. The FVPDM is performed by continuously injecting a tracer fluid into a well and monitoring the evolution of the tracer concentration into the same well. During all the experiment, the water column within this well is mixed to ensure a homogeneous repartition of the tracer mass. This method is originally based on a mathematical and a numerical model of tracer injection into a well, considered as a mass balance of the injection of tracer fluid and transit groundwater flow passing through the well screen (Brouyère, 2003). An analytical solution obtained from this model (Eq. (1)) was further applied as a single well tracer technique, enabling an accurate estimation of Darcy fluxes (Brouyère et al., 2008).

$$C_{w}(t) = \frac{Q_{in} \times C_{in} - \left(Q_{in} \times C_{in} - Q_{out} \times C_{w,0}\right) \times e^{-\frac{Q_{out}}{V_{w}} \times (t - t_{0})}}{Q_{out}} \text{ with }$$

$$Q_{out} = Q_{in} + Q_{t}^{in}$$
(1)

The tracer concentration within the well $C_w(t)$ [M L⁻³] can be calculated at each time t [T] using the parameters defined by the experimental setup C_{in} [M L⁻³] the tracer concentration in the injection solution, $C_{w,0}$ [M L⁻³] the tracer concentration within the well at initial time t_0 [T], Q_{in} [L³ T⁻¹] the tracer fluid injection flow rate and V_w [L³] the volume of water in the

injection well, assumed to be constant. Q_{out} [L³ T⁻¹], the flow rate leaving the well through the screen, carrying tracer at concentration C_w and representing the sum of Qin and Q_t^{in} [L³ T⁻¹] the transit flow rate intercepted by the well screen during tracer fluid injection at a rate Q_{in} . When $Q_{in} = 0$, $Q_t^{in} = Q_{out}$ and can be defined as Q_t , the transit flow rate under ambient conditions. Q_t is directly related to the Darcy's flux v [L T⁻¹] by the flow section A [L²] perpendicular to the groundwater flow. This area corresponds for fractured aquifer to the aperture of the fractures multiplied by the diameter of the borehole. $Q_t^{in} Q_t$ and v is related by the Eqs. (9) and (13) described in details in Brouyère et al., 2008.

Note that the dimensioning of a FVPDM experiment required an a priori estimation of a critical injection rate Q_{cr} [L³ T⁻¹] (Eq. (2)). If the tracer injection flow rate Q_{in} exceeds Q_{cr} , it induces a hydraulic loading of the well, which completely cancels the transit flow rate, making the experiment invalid.

$$Q_{cr} = \pi Q_t \tag{2}$$

During the experiment, the tracer concentration first increases in the injection well, until reaching a plateau when steady state conditions are observed between the rate of tracer injection and the rate of tracer that is carried out of the well by the groundwater flow. The experiment can thus be divided into three phases (Fig. 1). The first phase corresponds to transient concentrations and its duration is a function of the mixing volume V_w and the transit flow rate Q_t . The steady state conditions are reached faster if the mixing volume is small and the transit flow rate is high. The second phase begins when the concentration C_w in the well has stabilized, corresponding to steady state conditions. At this moment, C_w only depends on the tracer injection flow rate and on the transit flow rate (see Brouyère et al., 2008 Eq. 16 for more details). As a consequence, the interpretation of a FVPDM test consists in (1) calculating the transit flow rate from the steady state C_w and (2) in adjusting the mixing volume (V_w) to fit the transient phase of the experiment. Allowing the system to reach this steady state strongly increases the precision of the FVPDM interpretation because the two unknown parameters of the FVPDM equation

 $(V_w \text{ and } Q_t)$ can be determined independently on different parts of the experimental curve. At the end of the experiment, the injection of tracer is stopped and this last phase corresponds to a classical dilution.

Considering Eq. (1), the classical PDM (Eq. (3)) is only a specific case of the FVPDM, for $Q_{in}=0$ and $C_{w,0}>0$. C_w is related to the ratio of the transit flow rate on the mixing volume, in an exponential decay relation. This implies that the precision of the calculation of the transit flow rate (Q_t) fully relies on an accurate external estimation of the mixing volume (V_w). The transit flow rate could then be converted into a Darcy's flux v [L T^{-1}] by the flow section A [L^2] perpendicular to the undisturbed groundwater flow.

$$C_w(t) = C_{w,0} \times e^{-\frac{Q_t}{V_w}(t-t_0)}$$
 (3)

Considering the assumptions that are inherent to the classical PDM and FVPDM, both methods are affected by a priori limits. Classical PDM requires (1) steady state of the aquifer groundwater flow during a time sufficient for estimating $Q_{\rm t}$, (2) an homogeneous mixing of a large amount of the tracer in the water column instantaneous at the beginning and continuously during the experiment and (3) the accurate and precise knowledge of the mixing volume. The quality of FVPDM relies on the duration of the experiment. In the case of large mixing volume and/or limited groundwater flux, the FVPDM may require a long time to reach the steady state phase.

2.2. Experimental test site

The Stang Er Brune experimental test site is located at Ploemeur on the south coast of Brittany (France), in a crystalline rock aquifer constituted of micashists and granites (Fig. 2a). This site belongs to the H+ observatory (http://hplus.ore.fr/en/) which is a national network of highly instrumented research sites in subsurface hydrology. The site is equipped with three uncased, 0.12 m diameter wells of 80 to 100 m depth (B1, B2 and B3) and separated by less than 10 m and arranged in a triangular shape (Fig. 2b). At this location the contact between the micashists and the underlying granite is observed at about

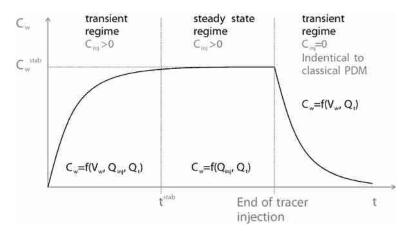


Fig. 1. Evolution of tracer concentrations (C_w) in a well where a FVPDM is performed. The steady state regime is reached when the mass flux of tracer injected in the well equilibrate with the mass flux of tracer flushed out of the well by the groundwater flow that transit by the well screen. The experiment ends as a classical PDM when the injection of tracer is stopped.

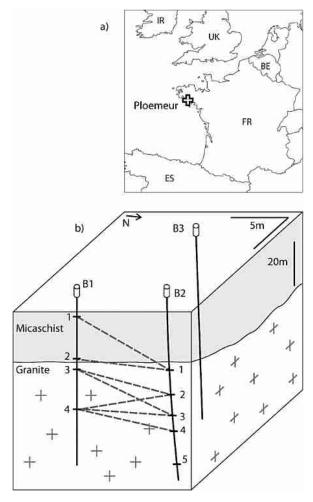


Fig. 2. a) Location of the Ploemeur test site. b) Configuration of the three 90 m deep wells (B1, B2, B3), and the fracture network. Dashed lines represent the hydraulic connections by group of fractures between B1 and B2 identified by tracer tests (Le Borgne et al., 2007; Dorn et al., 2012).

40 m below ground surface. The mean transmissivity obtained by various hydraulic tests in all the wells is around 10^{-3} m²/s (Le Borgne et al., 2006 and b). For the experiments described in this paper, two of the open boreholes (B1 and B2) were used. Wells B1 and B2 are intersected by 4 and 5 fracture zones, respectively, which are designated B1-1 to B1-4 and B2-1 to B2-5 (Fig. 2b).

This site offers several advantages. (1) The fractured aquifer has already been characterized by geophysical, thermal, hydraulic and tracer tests (Le Borgne et al., 2007; Dorn et al., 2012; Read et al., 2013). (2) Open boreholes without any casing are suitable for instrumentation with packers. (3) The small distances between the wells ensure a hydraulic connection that can be exploited for the purposes of the FVPDM experiments, i.e., to modify the transit flow rate Q_t in a given fracture set in the test well by pumping one of the other wells.

2.3. Double packer experimental setup

The experiments were performed in the deepest fracture zone identified in the well B1 (B1-4), where optical imagery showed two open fractures of 3 cm aperture in total at 78.7 m below the surface. The transmissivity of this fracture zone was estimated at 1.6×10^{-4} m²/s (Klepikova et al., 2014). The flow section A [L²] perpendicular to the direction of the groundwater flow is then 0.0036 m².

The experimental setup is designed to support FVPDM testing between a double packer system, which isolates the fracture zone (Fig. 3). Vertical borehole flows are prevented and the dilution experiment is carried out within the delineated space. The length of the test chamber between the upper and lower inflatable packer was 1.2 m. Pressure sensors were used to monitor piezometric head below, between and above the double packer in order to detect any leaky seals. A submersible pump was connected above the upper packer and linked to the test chamber to create a water circulation loop between the packers and the ground surface, where the loop was connected to a field fluorimeter, a pressure gauge, a water meter (to monitor flow rate of circulated water) and an electromagnetic pump for the low flow rate tracer injection. From the surface, the loop was completed at a connection allowing tracer injection at the bottom of the double packer test chamber (Fig. 3). The B2 well, located 6 m away from B1, was equipped with a submersible pump to impose the groundwater fluxes around B2 and in all the surrounding fractures, including the fractured zone identified in B1-4. The FVPDM-PDM experiments were performed for different pumping rates in well B2 in order to investigate the ability and limitations of the two dilution methods to measure different groundwater fluxes. B2 pumping rates ranged from 0 and 2.4×10^{-3} m³/s (0 to 144 L/min). Groundwater levels are also monitored in B2 and B3 wells using STS pressure sensors.

FVPDM experiments were performed under specified pumping flow rates in well B2. When the conditions have stabilized in the vicinity of wells (no pressure variations greater than 1 cm in 5 min), the tracer injection was started and the tracer concentration was monitored in the test chamber (thanks to the circulation loop). The circulation flow rate was precisely maintained at 4.2×10^{-5} m³/s (2.52 L/min) and the tracer injection at 3.5×10^{-7} m³/s (0.02 L/min) with a concentration of 207 ppb of fluoresceine (CAS no. 518-47-8). In total, a succession of 10 FVPDM (F1 to F10) and 8 classical PDM (P1 to P8) experiments was performed iteratively (Table 1). Mixing volume V_w and transit flow rate Q_t were then adjusted on the experimental data for each test separately. For the PDM experiments, an external estimations of V_w was used (i.e., independent of the interpretation of the exponential decay of tracer concentration observed during the PDM experiment). Uncertainties around adjusted values were estimated, and the results obtained for PDM and FVPDM compared and discussed.

2.4. Uncertainty estimation using a Bayesian approach

An adequate management of uncertainties is a critical issue in experimentation, and more generally in model calibration. Various sources of uncertainties co-exist (observations, experiment set up, simplified interpretation model) and might affect the parameter inference process. The Bayesian approach is a preferred method to perform inversion of nonlinear problems, and has been widely used to invert geophysical or hydrogeological data (e.g., Tarantola and Valette, 1982; Ghorbani

et al., 2007; Fasbender et al., 2008). This approach consists in propagating the knowledge provided by measurements m through a known and supposed to be exact forward model G (here the dilution Eqs. (1) and (3)), and to combine with an apriori knowledge of model parameters (here, mixing volume V_w and transit flow rate Q_t). Here, we will use a simplified definition of the posterior density function $p(\theta)$ for the parameter vector θ (Tarantola and Valette, 1982). It can be calculated from the a-priori probability density function $\mu(\theta)$

(here taken as uniform), the sum of squared residuals (SSR) between the model with parameter θ and observations m, as $SSR = \sum (m - G(\theta))^2$ and the standard deviation of measured data σ as

$$p(\theta) = \mu(\theta) \times e^{-\left(\frac{\sqrt{\text{SSR}(\theta)}}{2\sigma}\right)} \ . \tag{4}$$

Parameter uncertainties are finally computed as marginal probability density function.

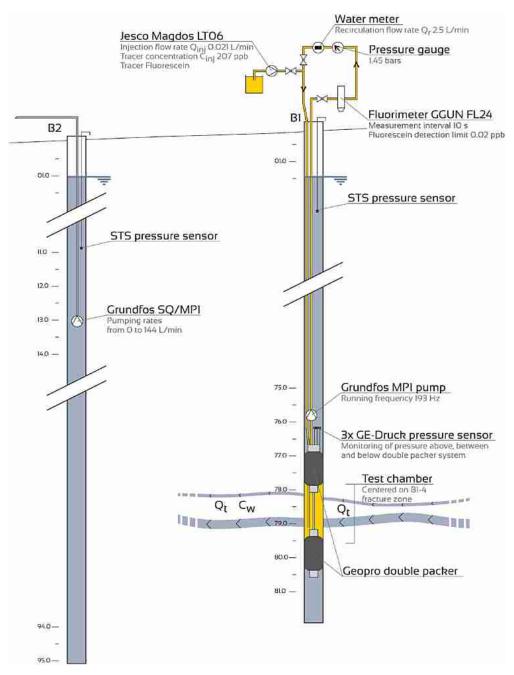


Fig. 3. Experimental setup limiting vertically the investigated fracture zone with double packers. The dilution tests are performed within this 1.2 m delineated test chamber. The corresponding volume of groundwater is mixed using a pump and circulated to the surface, where tracer is injected using a dosing pump. Concentration of tracer in the loop is monitored using a field fluorimeter placed in line. An immersed pump placed in the nearby well B2 allows the modification of the groundwater fluxes in the fracture B1-4. The aperture of the fractures is not at scale.

3. Results

Fig. 4 shows the experimental data of the succession of FVPDM–PDM tests conducted within the fracture B1-4 under different pumping rates in the nearby well B2. PDM experiments correspond to the periods when the tracer injection flow rate is null (Fig. 4b). The cumulated measurement time exceeds 100 h. As explained in previous sections, it is observed that the time to reach the steady state regime of FVPDM is longer when the pumping rate in B2, and thus the transit flow rates in fractures, decreases. The steady state concentration C_w^{stab} is also higher in this case, due to less important dilution effects.

Each phase of the experiment, corresponding to a specific pumping rate in the well B2 and to the PDM or FVPDM configuration, was interpreted separately. The adjustment of V_w and Q_t was performed by evaluating the RMS error between the experimental C_w values and the C_w values simulated using the analytical solutions of the PDM (Eq. (2)) and FVPDM (Eq. (1)).

3.1. Interpretation of a selected FVPDM and PDM experiment

Fig. 5 shows the results for the FVPDM and PDM experiment no. 3 (FVPDM 3 and PDM 3, see Table 1 for experimental setup parameters) for a specific pumping rate (Q_{pump}) of 1.5 \times 10⁻³ m³/s (90 L/min) in well B2. Fig. 5a shows the FVPDM experimental and simulated curves, which present the typical evolution of the tracer concentration with a transient phase at the beginning of the experiment and a steady state at the end of the test when the system has reached equilibrium. Fig. 5c is the RMS error plot between experimental data (FVPDM 3) and the simulated curves, obtained for different values of V_w and Q_t . The graph shows that a minimum RMS value is relatively well identified, corresponding to a unique (V_w , Q_t) pair that best fits the experimental data (Fig. 5a). These values are V_w equal to 35.6 L and Q_t equal to 7.43 \times 10⁻⁶ m³/s.

Fig. 5b and d is similar but corresponds to the PDM experiment no. 3. The experimental curve (Fig. 5b) shows the expected exponential decrease of the concentrations with time. However, with this method, it is rather difficult to adjust V_w and

 Q_t independently. A ratio Q_t/V_w of 2.12×10^{-4} s⁻¹ can be fitted on experimental results and, theoretically, a large range of couples (V_w, Qt) are possible. Accordingly, the RMS error obtained for the adjustment of V_w and Q_t (Fig. 5d) shows that a minimum RMS value cannot be identified and that the solution is not unique. Consequently, the mixing volume has to be precisely known to constrain the PDM model and to estimate the transit flow rate correctly.

Note that the values in the RMS plots depend on the data and duration of the experiments, but the shape of these plots will generally remain similar for longer experimental time.

3.2. External estimations of Vw for PDM interpretation

Estimating the actual mixing volume based on the characteristics of the experimental setup is difficult, mainly because of the geometry of the well, the use of the double packer system, the presence of equipment in the test chamber, and the use of circulation loop. It has been estimated to approximately 29 L, but the uncertainty on this value is unknown because the estimation was only based on the length and radius of the circulation pipes and on the dimension of the test chamber (radius of the well and distance between upper and lower packer when they are inflated) without taking into account the various equipment present within this delineated space. In this study, the actual mixing volume has been estimated using an alternative method based on an experimental artifact. At Fig. 5, PDM and FVPDM curves show oscillations (sequential plateaus) at the beginning of the experiment that attenuate with time. This artifact is due to a non-instantaneous mixing of tracer in the whole recirculated water volume. At the beginning or stopping of the tracer injection, a front of high or low concentration develops when the tracer injection is started or stopped. The mean wavelength of these oscillations has been estimated using Fourier transformations for all the dilution experiments and is equal to 762 s \pm 119 s (95% confidence interval). It actually corresponds to the time necessary for the water to travel the entire water circulation loop. Considering a circulation flow rate (Q_r) of 0.042 L/s, V_w equals 32 \pm 5 L.

Table 1Characteristics and sequence of tracer injections for FVPDM and PDM experiments on well B1-4. $C_{w,0}$ is the initial tracer concentration in well B1-4 at the beginning of the experiment. Q_{pump} corresponds to the pumping rate at well B2 and Q_{inj} to the tracer injection flow rate at a concentration C_{in} of 207 ppb.

ld Duration [h]		C _{w,0} in B1-4 [ppb]	Q_{in} in B1-4 [×10 ⁻⁷ m ³ /s]	Q_{pump} in B2 [$\times 10^{-3}$ m ³ /s]	
FVPDM 1	4.02	0	3.5	2.39	
PDM 1	0.88	5	0	2.39	
FVPDM 2	2.35	0.2	3.5	1.86	
PDM 2	2.28	6.1	0	1.86	
FVPDM 3	6.70	0.3	3.5	1.46	
PDM 3	1.67	9.2	0	1.46	
FVPDM 4	3.39	1.4	3.5	1.00	
FVPDM 5	2.83	12.5	3.5	0	
PDM 4	1.88	31.4	0	0	
PDM 5	2.24	30.3	0	1.00	
FVPDM 6	3.15	10.2	3.5	1.00	
FVPDM 7	8.67	14.1	3.5	0.63	
FVPDM 8	7.84	23.2	3.5	0	
PDM 6	5.93	68.0	0	0	
PDM 7	2.45	64.9	0	0.63	
FVPDM 9	28.01	2.4	3.5	0.31	
FVPDM 10	8.72	45.1	3.5	0.62	
PDM 8	2.10	23.5	0	0.29	

Using this value, the transit flow Q_t rate can be calculated from PDM experiments. For PDM no. 3 experiment, it is equal to 6.82×10^{-6} m³/s. Both values for V_w (32 L) and Q_t (6.82 × 10⁻⁶ m³/s) agree with FVPDM estimates (V_w = 35.6 L and Q_t = 7.43 × 10⁻⁶ m³/s) within 10% of error.

3.3. Evaluation of uncertainties on the adjustment of V_w and Q_t for a selected FVPDM and PDM test

Both FVPDM and PDM can be used to estimate groundwater fluxes within the B1-4 fracture zone. However, the two methods are different and the confidence to be attributed to the results has to be determined. The uncertainties on calculated fluxes are related to the adjustment of the analytical solutions on experimental data and to the confidence on the V_w value, in the case of the PDM. The analysis of uncertainties is based on the exploration of Q_t and V_w values between specified intervals, using Eqs. (1) and (2). The RMS errors between the experimental and simulated C_w values have been converted into probabilities according to Eq. (4) (see Section 2.4).

The probabilities are calculated for the FVPDM and PDM experiment no. 3. They are multiplied with the normal distribution related to the estimation of V_w , equal to $32~{\rm L}\pm 5~{\rm L}$, to draw the probability plots presented in Fig. 6. These plots are further used to calculate the most probable value for V_w and Q_r and the 95% confidence intervals (Table 2), for both PDM and FVPDM. Considering the results related to the experiment no. 3, the 95% confidence interval on the calculated transit flow rate is more than five times smaller for the FVPDM than for the PDM. These methodology and results are also dependent on the respective durations of the experiments, which are not equivalent in this case. To conclude about the general performances of both methods, the issues related to the duration

of the different experiments are further discussed in the next section.

3.4. Influence of the duration of the experiment

The accuracy of the adjusted values for the PDM and FVPDM increases with the duration of the experiment. Concerning the FVPDM, this accuracy reaches a maximum value when the tracer concentration has stabilized in the injection well. The time to reach this steady state increases as the mixing volume increases and the transit flow rate decreases. To compare the FVPDM and PDM including the 'time' issue, uncertainties on the adjusted Q_t are investigated as a function of a normalized experiment duration. A normalized time t^* independent of V_w and Q_t is used and is obtained by dividing the mixing volume V_w by the critical injection flow rate Q_{cr} (see Section 2.1).

$$t^* = \frac{V_w}{Q_{cr}} = \frac{V_w}{\pi \times Q_t} \tag{5}$$

The uncertainty around Q_t^0 has been calculated for the FVPDM and PDM experiment no. 3, but by artificially considering on specific fractions of the available experimental data, corresponding to specific numbers of t^* (Fig. 7). Considering Eq. (1), the critical time t_c , necessary to reach 99% of the steady state concentration, is reached after 13.9 t^* . If Q_{in} is small enough and neglected in comparison to Q_t , this critical time tends to 14.5 t^* . This is in accordance with the results shown in Fig. 7. The total duration of the FVPDM no. 3 is 16.8 t^* . The corresponding non-dimensional time for the PDM no. 3 allowed only a duration of 4.5 t^* .

The uncertainty (P05–P95) around the calculated transit flow rate Q_t decreases significantly with time for the FVDPM. The FVPDM is less precise for the determination of Q_t for short

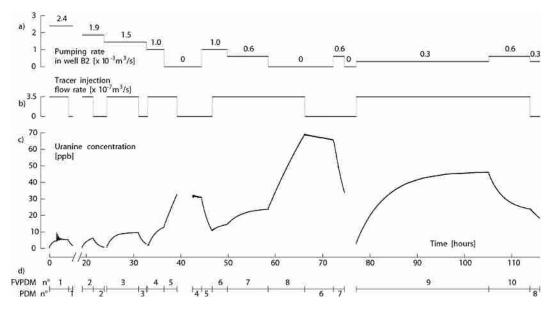


Fig. 4. Evolution of tracer concentration (c) during the measurement of groundwater flow by FVPDM and PDM in the B1-4 fracture. The distinction between natural and forced hydraulic conditions is represented by the pumping rate applied in the well B2 (a). The distinction between FVPDM and PDM experiments is figured by the tracer injection flow rate (b), PDM being performed when Q_{in} is null. Discontinuity in the measurement of tracer concentration is due to stops of the fluorimeter during equipment manipulations. Spike of tracer concentration during FVPDM no. 1 is due to a technical problem but does not prevent the interpretation of the test. The identification numbers of the FVPDM and PDM successive experiments are named in Fig. 4d.

experiment durations (t lower that approximately 4 t* or 0.29 t_c) and clearly overestimates the value of Q_t . In this field campaign, this is partly explained by the non-uniform mixing of tracer in the circulated volume, which disturbed the increase of tracer concentration at the beginning of the experiment. It also comes from the time required for a good estimate. But for long experiment, the accuracy of measurements becomes very good, with an uncertainty less than 10% of Qt, for duration higher than 10 t^* or 0.72 t_c . Concerning the classical PDM, the uncertainty also decreases with time due to the attenuation of oscillations in tracer concentration at the beginning of the dilution and but seems to stay relatively high, around 25% of Q_t. But this uncertainty is only dependent on the precision of the externally estimated V_w (see previous sections). Although the uncertainty is relatively high, the mean estimates are acceptable for all times including short times.

Whatever the duration of the PDM test, a complete FVPDM (i.e., a FVPDM that reaches the steady state) is more precise. The 'threshold time', when the FVPDM becomes more precise

than the PDM is in this case equal to 0.29 t_c , but it depends on the precision of the externally estimated V_w used in the PDM experiments, and increases as V_w is more accurately estimated.

3.5. Comparison of results for different fracture flow rates

All the dilution experiments have been interpreted separately, considering an a priori estimated mixing volume of 32 \pm 5 L and an unknown transit flow rate. Results are presented in Table 3 and in Fig. 8. The critical time t_c corresponds to the time necessary to reach 99% of the FVPDM steady state tracer concentration. It is estimated from Eq. (1) considering that the initial tracer concentration is zero. This critical time can be compared to the actual duration of each experiment to estimate if steady state has been reached.

The relationship between the transit flow rate in the fracture B1-4 determined by both FVPDM and PDM and the pumping rate applied in B2 (Fig. 8) appears to be linear. A slight deviation may be observed for the highest pumping rates, but

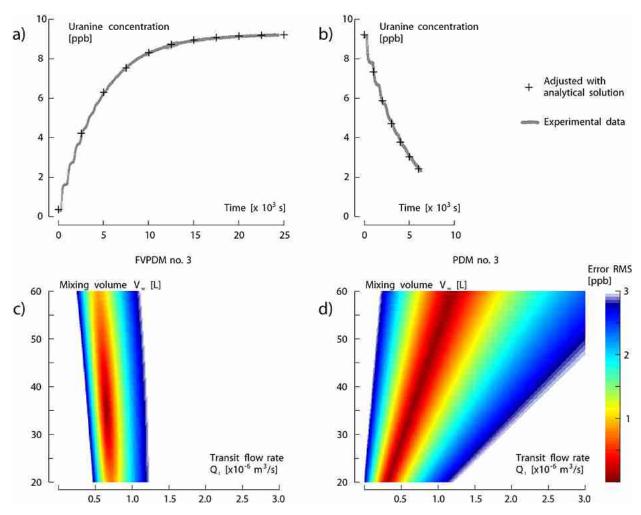


Fig. 5. Experimental data (gray points) and adjusted analytical solutions (black crosses) of FVPDM no. 3 (a) and PDM no. 3 (b) experiments corresponding to a pumping rate of 1.5×10^{-3} m³/s (90 L/min) in the B2 well. (c) and (d) are the RMS error plot for the FVPDM and PDM experiments for the adjustment of the mixing volume and the groundwater transit flow rate. A unique pair of Q_t/V_w value fits the FVPDM equation ($V_w = 35.6$ L, $Q_t = 7.43 \times 10^{-6}$ m³/s). On the contrary, a wide range of Q_t/V_w pairs that satisfies the PDM equation without being able to determine a most probable one ($Q_t/V_w = 2.12 \times 10^{-4}$ s⁻¹). Note the oscillations of tracer concentration in the well (sequential plateaus) at the beginning of FVPDM and PDM experiment.

this is difficult to confirm, given the calculated uncertainties (see discussion below). However, the relationship between the drawdown and the pumping rate in B2 (data Table 3) also presents a slight deviation from the linear behavior, suggesting that flow in the system may not be fully Darcyan.

The adjusted transit flow rates for all the dilution experiments are always higher for the FVPDM (hollow circles) than for the PDM (gray squares), but the confidence intervals are intersecting. Concerning the PDM, the information on the mixing volume is only provided externally (in this case, thanks to the oscillations artifacts), and it impacts the estimation of the transit flow rate. The bias between FVPDM and PDM results (Fig. 8 and Table 3) can be explained by underestimation of this mixing volume. This volume was estimated to 29 L based on geometric characteristics, to 32 \pm 5 L based the oscillations in the experimental curves (Section 3.2), and a bit higher for the most accurate FVPDM experiments (FVPDM 3 and FVPDM 9 in Table 3). If the PDM is interpreted using a higher value for V_w , as suggested by the most accurate FVPDM tests, the adjusted Q_t converge for the FVPDM and PDM tests. This is indeed logical since the PDM is only the last part of a full FVPDM experiment. This also illustrates the need for precise external estimation of V_w , if using PDM experiments only. This level of precision is however not always possible.

The FVPDM generally presents a better precision with smaller confidence intervals, which increase with the calculated transit flow rate and pumping flow rate in well B2 (Fig. 8). The differences are due to a higher sensitivity of the FVPDM to the experimental data, and because the FVPDM is also able to provide an independent information on both transit flow rate and mixing volume. In this case, the results of Table 3 show that the adjusted V_w varies for the different FVPDM experiments. These variations of adjusted V_w can be due to the oscillations of tracer concentrations that disturb the rising part of the FVPDM curve and observation errors. This is precisely the part of the curve which is used to adjust the value of the mixing volume. This is particularly the case when the duration of the FVPDM experiment that has not last enough to reach the steady state and therefore limit the precision of the adjustments of V_w and Q_t , as explained in previous sections.

The transit flow rate estimated for the FVPDM no. 2 carried out with a pumping rate of 1.86×10^{-3} m³/s at well B2 presents a more important uncertainty and appears to deviate, compared to the other FVPDM experiments. This can be explained by a short experiment duration (see Section 3.4 and Table 3) of only $0.64\ t_{\rm c}$, leading to more uncertainty and potential errors. Note that the results of FVPDM no. 1 are also affected by some 'noise' in the experimental data (see Fig. 4), due to a technical problem, leading to more uncertainty.

No transit flow rate could be calculated for the FVPDM no. 5 and no. 8 performed with no pumping at the well B2 (i.e., under natural ambient groundwater flow in the aquifer). Under these slow groundwater flow conditions, the critical flow rate determined by the PDM nos. 4 and 6 is around 2×10^{-7} m³/s. The injection of tracer at a rate of 3.5×10^{-7} m³/s (the lowest that can be achieved with the available equipment) exceeds thus the critical injection rate Q_{cr} making the experiment invalid as explained in Section 2.1. With the available acer injection pump and an injection flow rate Q_{in} of 6×10^{-8} m³/s, t_c would have been around 10 days.

4. Discussion

A comparison of the present results with the experiments of Novakovski (2006) that performed PDM between packer shows that the FVPDM experimental setup used during this field campaign can investigate a range of Darcy's flux transit flow rate higher than Novakowski's PDM. Nevertheless the FVPDM offers a distinct estimation of V_w that is unavailable with the PDM. The measurement of fracture flow velocities of Novakowski ranges from 1.2×10^{-5} to 4.5×10^{-3} m/s, the present FVPDM performed at Ploemeur measured fractures flow from 3.1×10^{-3} to 3.8×10^{-2} m/s.

Considering these experimental data for dilution experiment no. 3, the FVPDM becomes more precise than the PDM from a time corresponding to approximately 4 t^* or 0.29 t_c . This result is consistent with the initial recommendation of Brouyère et al. (2008) that recommended an experiment duration of 5 to 7 times t^* . to ensure reaching the steady state of the FVPDM. The same calculation has been carried out for all

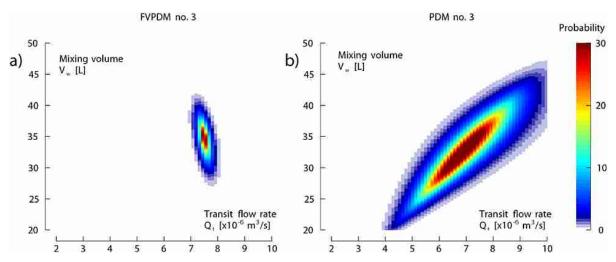


Fig. 6. Adjustment of V_w and Q_t for the experiment no. 3 (with pumping at 1.5×10^{-3} m³/h in B2) considering an a priori known V_w of 32 ± 5 L.

Table 2 Results of the adjustment of the parameters Q_t and V_w considering a probability density function on V_w of 32 \pm 5 L for PDM and FVPDM experiment no. 3.

	$Q_t [\times 10^{-6} \text{ m}^3/\text{s}]$			V _w [L]				
	Adjusted	P05	P95	P95-P05	Adjusted	P05	P95	P95-P05
FVPDM 3 PDM 3	7.55 6.82	7.19 5.11	7.89 9.12	0.70 4.01	34.0 32.2	29.2 25.3	38.0 41.2	8.8 15.9

the dilution tests and shows identical trends with the precision on the adjusted Q_t increasing with time for FVPDM. This precision remains high for PDM, whatever the duration of the experiment, but mainly depends on the accuracy of the external estimation of V_w . As a conclusion, classical PDM seems to be a technique suitable for rapid results, including a large range of groundwater fluxes. However, this study has highlighted the crucial need for accuracy regarding the a priori knowledge of V_w when accuracy using PDM experiments. This accuracy actually directly affects the performance and possible bias of PDM results. At the contrary, the FVPDM is more precise, even without estimation of V_w , but may require long experiment durations under specific conditions. In case of very slow groundwater flow and large mixing volume, the time required to reach steady state may actually become very long and unmanageable. For example, if the transit flow rate Q_t is lower than 10^{-7} m³/s and the mixing volume is higher than 10 L simultaneously, the time to reach the critical time t_c (or 5 t^*) exceeds 48 h. Furthermore, the estimation of the mixing volume V_w by the FVPDM is more robust than simply by using the geometry of the well. Vw determined by FVPDM is an apparent value that takes into account all the water that participates to the mixing of tracer. For example it can integrate an unknown dead-end fracture that would not be considered with a classic PDM and bias the result of the transit flow rate.

Considering the results of Table 3, the ratio between the transit flow rate calculated with FVPDM and the pumping flow rate in B2, ranges between 170 and 230, approximately. If the fluxes are assumed uniformly distributed around B2, this ratio should be equal to 754. This last value is obtained by considering the following values. The distance between B1 and B2 is equal to 6 m. Calculated flow rates correspond to a 0.1 m section (the diameter of B1) of the circle

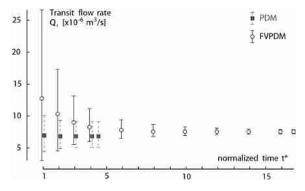


Fig. 7. Evolution of the calculated Q_t and the 95% confidence intervals, as a function of the duration of the experiment for FVPDM no. 3 (hollow circles) and PDM no. 3 (gray squares) (pumping rate of $1.5 \times 10^{-3} \text{ m}^3/\text{s}$ in B2). t^* corresponds to a normalized time allowing the comparison between dilution experiments with different transit flow rates.

intercepting B1, and having B2 as a center. Finally, only 50% the total pumping flow rate in B2 is coming from the B1-4 fracture. This was evidenced by Read et al. (2013) using heat tracer tests. The lower experimental ratio, compared to the theoretical ratio, highlights the fact that fluxes are more probably non-uniform within the fractures, for example with some possible channelization.

From a practical point of view, an improvement of the experimental setup could be to get rid of the circulation loop by placing all the surface equipment (tracer injection pump, fluorimeter and mixing propeller) into the test chamber. In this case, the water present in the loop represents 25% of the total mixing volume. Such a reduction of V_w would significantly decrease the time to reach a steady state for the FVPDM and avoid the oscillatory effect of the circulation of tracer along the loop. The use of a dosing pump with smaller minimum tracer injection rate would also allowed for determination of smaller transit flow rate such as in natural flow conditions. Moreover, an inflatable double packer of this size (more than 4 m) is not easy to use in the field and requires heavy equipment to be installed in the well. The development of a specific probe gathering all the required equipment into a compact size device will also improve the practicality of the method.

The FVPDM nos. 4 and 5; 6, 7 and 8; and 9 and 10 were performed consecutively by maintaining the injection of tracer and changing the pumping rate at the nearby well. The changes in the groundwater flow velocity were recorded by those continuous FVPDM experiments. This highlights that the FVPDM is capable of monitoring temporal changes of groundwater flow. On the contrary, a variable groundwater flux precludes the interpretation of classical PDM because this method is based on the hypothesis that the groundwater flux is constant. Development of the FVPDM for long term monitoring of transient groundwater flow constitutes the most interesting perspective. For that, the experimental setup has to be optimized by reducing the tracer injection flow rate to avoid frequent refill of the tracer solution tank. And finally a mathematical model has to be developed to interpret the FVPDM experiment in case of transient groundwater flow.

5. Conclusions

The finite volume point dilution method has been applied to measure groundwater fluxes within a local fracture zone of the crystalline aquifer of Ploemeur, France. This manipulation is the first successful application of the FVPDM technique in a fractured aquifer and using a double packer system. Experiments have been carried out for variable groundwater flow, induced by pumping in a well located close to the tested well. In total, 10 FVPDM and 8 classical PDM were performed to compare the two methods.

Measurements of groundwater fluxes by classical PDM provide good estimates, even for short times experiments, if V_w

Table 3 Result of the dilution experiments carried out on B1-4. Uncertainties on V_w and Q_t correspond to the calculated confidence interval at 95%. t_c is the critical time necessary to reach 99% of the steady state concentration (* not interpretable).

Id	Data			Results				
	Duration [h]	Q_{pump} in B2 [×10 ⁻³ m ³ /s]	Drawdown B2 [m]	Drawdown B1 [m]	Duration/ t_c [$-$]	$Q_t \left[\times 10^{-6} \text{ m}^3/\text{s} \right]$	V _w [L]	$v [\times 10^{-3} \text{ m/s}]$
FVPDM 1	4.02	2.39	1.89	0.88	1.35	13.80 ± 1.21	32.9 ± 5.5	38.33 ± 3.36
PDM 1	0.88	2.39	1.89	0.88		10.69 ± 3.66	32.5 ± 7.9	29.69 ± 10.17
FVPDM 2	2.35	1.86	1.30	0.60	0.64	11.6 ± 1.80	34.5 ± 6.5	32.22 ± 5
PDM 2	2.28	1.86	1.30	0.60		8.56 ± 2.63	32.4 ± 7.9	23.78 ± 7.31
FVPDM 3	6.7	1.46	0.98	0.44	1.22	7.55 ± 0.35	34.0 ± 4.4	20.97 ± 0.97
PDM 3	1.67	1.46	0.98	0.44		6.82 ± 2.00	32.2 ± 7.9	18.94 ± 5.56
FVPDM 4	3.39	1.00	0.62	0.31	0.48	4.83 ± 0.83	28.8 ± 5.4	13.42 ± 2.31
PDM 5	2.24	1.00	0.68	0.37		4.25 ± 1.16	32.4 ± 7.9	11.81 ± 3.22
FVPDM 6	3.15	1.00	0.68	0.37	0.43	4.60 ± 0.23	28.2 ± 6.4	12.78 ± 0.64
FVPDM 7	8.67	0.63	0.36	0.17	0.67	2.78 ± 0.08	31.7 ± 4.4	7.72 ± 0.22
PDM 7	2.45	0.63	0.41	0.21		2.33 ± 0.66	32.5 ± 7.9	6.47 ± 1.83
FVPDM 10	8.72	0.62	0.38	0.17	0.64	2.93 ± 0.17	34.8 ± 6.0	8.14 ± 0.47
FVPDM 9	28.01	0.31	0.13	0.03	1.09	1.32 ± 0.04	33.5 ± 2.5	3.67 ± 0.11
PDM 8	2.1	0.29	0.17	0.06		1.20 ± 0.32	32.7 ± 7.9	3.33 ± 0.89
FVPDM 5	2.83	0	0.04	0.02	0.03	*	27.0	*
PDM 4	1.88	0	0.04	0.02		0.22 ± 0.09	32.5 ± 10.2	0.61 ± 0.25
FVPDM 8	7.84	0	0.06	0.02	0.07	*	32.0	*
PDM 6	5.93	0	0.06	0.02		0.07 ± 0.02	32.7 ± 7.9	0.19 ± 0.06

can be precisely estimated. With this method, the precision on the calculated groundwater flux fully depends on the precision of the estimation of the water circulation volume. On the contrary, the FVPDM allows for an independent estimation of both groundwater flow rate Qt and water mixing volume V_w . The best precision is obtained when steady state conditions are reached for tracer concentration in the tested well, which may require long experimental durations. Classical PDM seems to be more accurate than FVPDM for short experiments provided the mixing volume is accurately known. FVPDM generally provides a better accuracy but requires longer experiment durations.

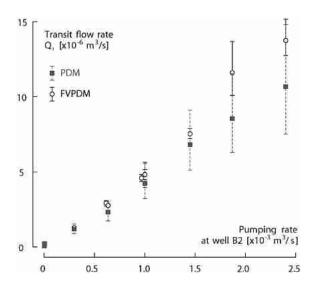


Fig. 8. A linear relation is observed between the pumping rate applied in the well B2 and the groundwater flow rate observed in the fracture B1-4. The transit flow rate (Q_t) adjusted for all the dilution experiments are always higher for the FVPDM (hollow circles) than for the PDM (gray squares) due to difference of adjusted V_w and 95% confidence intervals are always shorter for FVPDM than PDM.

The 'threshold' after which FVPDM becomes more accurate than PDM depends on the precision reached in the external estimation of the mixing volume.

The present experiments also highlight the ability of the FVPDM to continuously monitor continuous transient ground-water fluxes. Two short term perspectives could be (1) to develop a mathematical model to interpret a fully transient FVPDM test and (2) to follow a multiple stages pumping test performed at a well with FVPDM monitoring at some nearby piezometer to investigate the benefits of groundwater fluxes information in the interpretation of pumping tests.

In conclusion, both methods are complementary and can investigate the same range of groundwater fluxes. The classical PDM should be used for rapid estimation of steady state groundwater flux. The FVPDM is a more precise method but requires longer duration experiment to achieve a good precision if the investigated groundwater fluxes are low and/or if the mixing volume is large, and has a strong development potential for monitoring of transient groundwater fluxes.

Acknowledgments

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